

$$\ker(\phi) \leq \pi_1(D_n)$$