

$$\beta_{*}:\pi_1(D_n)\longrightarrow \pi_1(D_n)$$